
grmpy Documentation

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Development Team

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`grmpy` is an open-source package for the simulation and estimation of the generalized Roy model. It serves as a teaching tool to promote the conceptual framework of the generalized Roy model, illustrate a variety of issues in the econometrics of policy evaluation, and showcase basic software engineering practices.

We build on the following main references:

James J. Heckman and Edward J. Vytlačil. [Econometric evaluation of social programs, part I: Causal models, structural models and econometric policy evaluation](#). In *Handbook of Econometrics*, volume 6B, chapter 70, pages 4779–4874. Elsevier Science, 2007.

James J. Heckman and Edward J. Vytlačil. [Econometric evaluation of social programs, part II: Using the marginal treatment effect to organize alternative econometric estimators to evaluate social programs, and to forecast their effects in new environments](#). In *Handbook of Econometrics*, volume 6B, chapter 71, pages 4875–5143. Elsevier Science, 2007.

Jaap H. Abbring and James J. Heckman. [Econometric evaluation of social programs, part III: Distributional treatment effects, dynamic treatment effects, dynamic discrete choice, and general equilibrium policy evaluation](#). *Handbook of Econometrics*, volume 6B, chapter 72, pages 5145-5303. Elsevier Science, 2007.

The remainder of this documentation is structured as follows. We first present the basic economic model and provide installation instructions. We then illustrate the basic use case of the package in a tutorial and showcase some evidence regarding its reliability. In addition we provide some information on the software engineering tools that are used for transparency and dependability purposes. The documentation concludes with further information on contributing, contact details as well as a listing of the latest releases.

The package is used as a teaching tool for a course on the analysis human capital at the University of Bonn. The affiliated lecture material is available on [GitHub](#) .

This section provides a general discussion of the generalized Roy model and selected issues in the econometrics of policy evaluation.

1.1 Generalized Roy Model

The generalized Roy model ([18], [28]) provides a coherent framework to explore the econometrics of policy evaluation. It is characterized by the following set of equations.

Potential Outcomes

$$Y_1 = \mu_1(X) + U_1$$

$$Y_0 = \mu_0(X) + U_0$$

Choice

$$D^* = \mu_D(Z) - V$$

$$D = I[D^* > 0]$$

$$B = E[Y_1 - Y_0 | \mathcal{I}]$$

Observed Outcome

$$Y = DY_1 + (1 - D)Y_0$$

(Y_1, Y_0) are objective outcomes associated with each potential treatment state D and realized after the treatment decision. Y_1 refers to the outcome in the treated state and Y_0 in the untreated state.

D^* denotes the latent tendency for treatment participation. It includes any subjective benefits, e.g. job amenities, and costs, e.g. tuition costs. Agents take up treatment D if their latent tendency D^* is positive. \mathcal{I} denotes the agent's information set at the time of the participation decision. The observed outcome Y is determined in a switching-regime fashion ([25], [26]). If agents take up treatment, then the observed outcome Y corresponds to the outcome in the presence of treatment Y_1 . Otherwise, Y_0 is observed. The unobserved potential outcome is referred to as the counterfactual outcome. If costs are identically zero for all agents, there are no observed regressors, and $(U_1, U_0) \sim N(0, \Sigma)$, then the generalized Roy model corresponds to the original Roy model ([28]).

From the perspective of the econometrician, (X, Z) are observable while (U_1, U_0, V) are not. X are the observed determinants of potential outcomes (Y_1, Y_0) , and Z are the observed determinants of the latent indicator variable D^* . The Potential outcomes as well as the latent indicator D^* are decomposed into their means $(\mu_1(X), \mu_0(X), \mu_D(Z))$ and their deviations from the mean (U_1, U_0, V) . (X, Z) might have common elements. Observables and unobservables jointly determine program participation D .

If their ex ante latent indicator for participation D^* is positive, then agents select into treatment. Yet, this does not require their expected objective benefit B to be positive as well. Note that the unobservable term V enters D^* with a negative sign. Therefore conditional on Z , high values of V indicate a lower propensity for selecting into treatment and vice versa.

The evaluation problem arises because either Y_1 or Y_0 is observed. Thus, the effect of treatment cannot be determined on an individual level. If the treatment choice D depends on the potential outcomes, then there is also a selection problem. If that is the case, then the treated and untreated differ not only in their treatment status but in other characteristics as well. A naive comparison of the treated and untreated leads to misleading conclusions. Jointly, the evaluation and selection problem are the two fundamental problems of causal inference ([21]). Using the setup of the generalized Roy model, we now highlight several important concepts in the economics and econometrics of policy evaluation. We discuss sources of agent heterogeneity and motivate alternative objects of interest.

1.2 Agent Heterogeneity

What gives rise to variation in choices and outcomes among, from the econometrician's perspective, otherwise observationally identical agents? This is the central question in all econometric policy analyses ([5], [11]).

The individual benefit of treatment is defined as

$$B = Y_1 - Y_0 = (\mu_1(X) - \mu_0(X)) + (U_1 - U_0).$$

From the perspective of the econometrician, differences in benefits are the result of variation in observable X and unobservable characteristics $(U_1 - U_0)$. However, $(U_1 - U_0)$ might be (at least

partly) included in the agent's information set \mathcal{I} and thus known to the agent at the time of the treatment decision. Therefore we are able to distinguish between observable and unobservable heterogeneity. Observable heterogeneity is reflected by the difference $\mu_1(X) - \mu_0(X)$. t denotes the differences between individuals that are based on differences of observable individual specific characteristics captured by X . Since we are able to take observable heterogeneity into account by conditioning on X this kind of heterogeneity is a negligible problem for the evaluation of policy interventions. Therefore all following concepts condition on X .

Consequently the second type of heterogeneity is represented by the differences between individuals captured by $U_1 - U_0$. This differences are unobservable from the perspective of an econometrician. It should be noted that the term *unobservable* does not implicate that U_1 and U_0 are not completely or at least partly included in an individual's information set. As a result, unobservable treatment effect heterogeneity can be distinguished into private information and uncertainty. Private information is only known to the agent but not the econometrician; uncertainty refers to variability that is unpredictable by both.

The information available to the econometrician and the agent determines the set of valid estimation approaches for the evaluation of a policy. The concept of essential heterogeneity emphasizes this point ([16]). If agents select their treatment status based on benefits unobserved by the econometrician (selection on unobservables), then there is no unique effect of a treatment or a policy even after conditioning on observable characteristics. In terms of the Roy model this is characterized by the following condition

$$Y_1, Y_0 \not\perp D$$

Average benefits are different from marginal benefits, and different policies select individuals at different margins. Conventional econometric methods that only account for selection on observables, like matching ([7], [13], [27]), are not able to identify any parameter of interest ([16], [18]). For example, [6] present evidence on agents selecting their level of education based on their unobservable gains and demonstrate the importance of adjusting the estimation strategy to allow for this fact. [14] propose a variety of tests for the the presence of essential heterogeneity.

1.3 Objects of Interest

Treatment effect heterogeneity requires to be precise about the effect being discussed. There is no single effect of neither a policy nor a treatment. For each specific policy question, the object of interest must be carefully defined ([18], [19], [20]). We present several potential objects of interest and discuss what question they are suited to answer. We start with the average effect parameters. However, these neglect possible effect heterogeneity. Therefore, we explore their distributional counterparts as well.

1.3.1 Conventional Average Treatment Effects

It is common to summarize the average benefits of treatment for different subsets of the population. In general, the focus is on the average effect in the whole population, the average treatment effect B^{ATE} , or the average effect on the treated B^{TT} or untreated B^{TUT} .

$$\begin{aligned}
 B^{ATE} &= E[Y_1 - Y_0] \\
 B^{TT} &= E[Y_1 - Y_0 | D = 1] \\
 B^{TUT} &= E[Y_1 - Y_0 | D = 0]
 \end{aligned}$$

All average effect parameter possibly hide considerable treatment effect heterogeneity. The relationship between these parameters depends on the assignment mechanism that matches agents to treatment. If agents select their treatment status based on their own benefits, like in the presence of essential heterogeneity, then agents that take up treatment benefit more than those that do not and thus $B^{TT} > B^{ATE}$. If agents select their treatment status at random, which is equivalent with the absence of essential heterogeneity, then all parameters are equal. Figure 1 illustrates an example for both cases. Both graphs show the distribution of benefits which is characterized by the difference of potential outcomes $Y_1 - Y_0$. Additionally the figures shows the conventional effects for both setups whereupon the selection process on the left side is affected by essential heterogeneity whereas the right side displays the effects in the absence of essential heterogeneity.

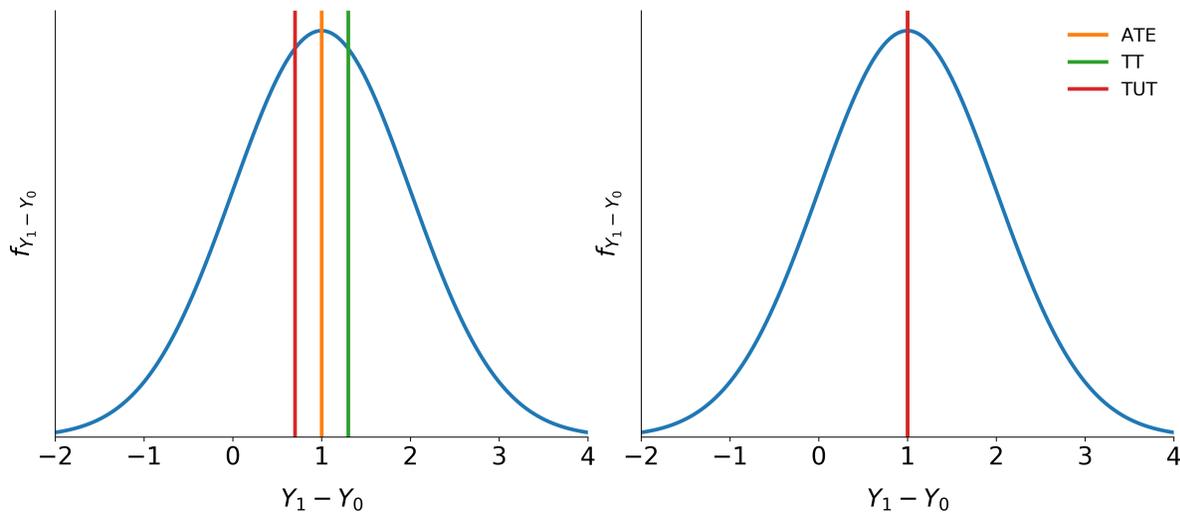


Fig. 1: **Fig. 1:** Conventional treatment effects with and without essential heterogeneity

The policy relevance of the conventional treatment effect parameters is limited in the presence of essential heterogeneity. They are only informative about extreme policy alternatives. The B^{ATE} is of interest to policy makers if they weigh the possibility of moving a full economy from a baseline to an alternative state or are able to assign agents to treatment at random. The B^{TT} is informative if the complete elimination of a program already in place is considered. Conversely, if the same program is examined for compulsory participation, then the B^{TUT} is the policy relevant parameter.

To ensure a tight link between the posed policy question and the parameter of interest, [17] propose the policy-relevant treatment effect $B^{P RTE}$. They consider policies that do not change potential outcomes, but only affect individual choices. Thus, they account for voluntary program participation.

1.3.2 Policy-Relevant Average Treatment Effect

The $B^{P RTE}$ captures the average change in outcomes per net person shifted by a change from a baseline state B to an alternative policy A . Let D_B and D_A denote the choice taken under the baseline and the alternative policy regime respectively. Then, observed outcomes are determined as

$$\begin{aligned} Y_B &= D_B Y_1 + (1 - D_B) Y_0 \\ Y_A &= D_A Y_1 + (1 - D_A) Y_0. \end{aligned}$$

A policy change induces some agents to change their treatment status ($D_B \neq D_A$), while others are unaffected. More formally, the $B^{P RTE}$ is then defined as

$$B^{P RTE} = \frac{1}{E[D_A] - E[D_B]} (E[Y_A] - E[Y_B]).$$

As an example consider that policy makers want to increase the overall level of education. Rather than directly assigning individuals a certain level of education, policy makers can only indirectly affect schooling choices, e.g. by altering tuition cost through subsidies. The individuals drawn into treatment by such a policy will neither be a random sample of the whole population, nor the whole population of the previously (un-)treated. Therefore the implementation of conventional effects run the risk of being biased, whereas the $B^{P RTE}$ is able to evaluate the average change in outcomes per net individual that is shifted into treated.

1.3.3 Local Average Treatment Effect

The Local Average Treatment Effect $B^{L ATE}$ was introduced by [24]. They show that instrumental variable approaches (IV) identify $B^{L ATE}$, which measures the mean gross return to treatment for individuals induced into treatment by a change in an instrument.

Unfortunately, the people induced to go into treatment by a change in any particular instrument need not to be the same as the people induced to select into treatment by policy changes other than those corresponding exactly to the variation in the instrument. A desired policy effect may be directly correspond to the variation in the instrument. Moreover, if there is a vector of instruments that generates choice and the components of the vector are intercorrelated, IV estimates using the components of Z as the instruments, one at a time, do not, in general, identify the policy effect corresponding to varying that instruments, keeping all other instruments fixed, the ceteris paribus effect of the change in the instrument. [12] develop this argument in detail.

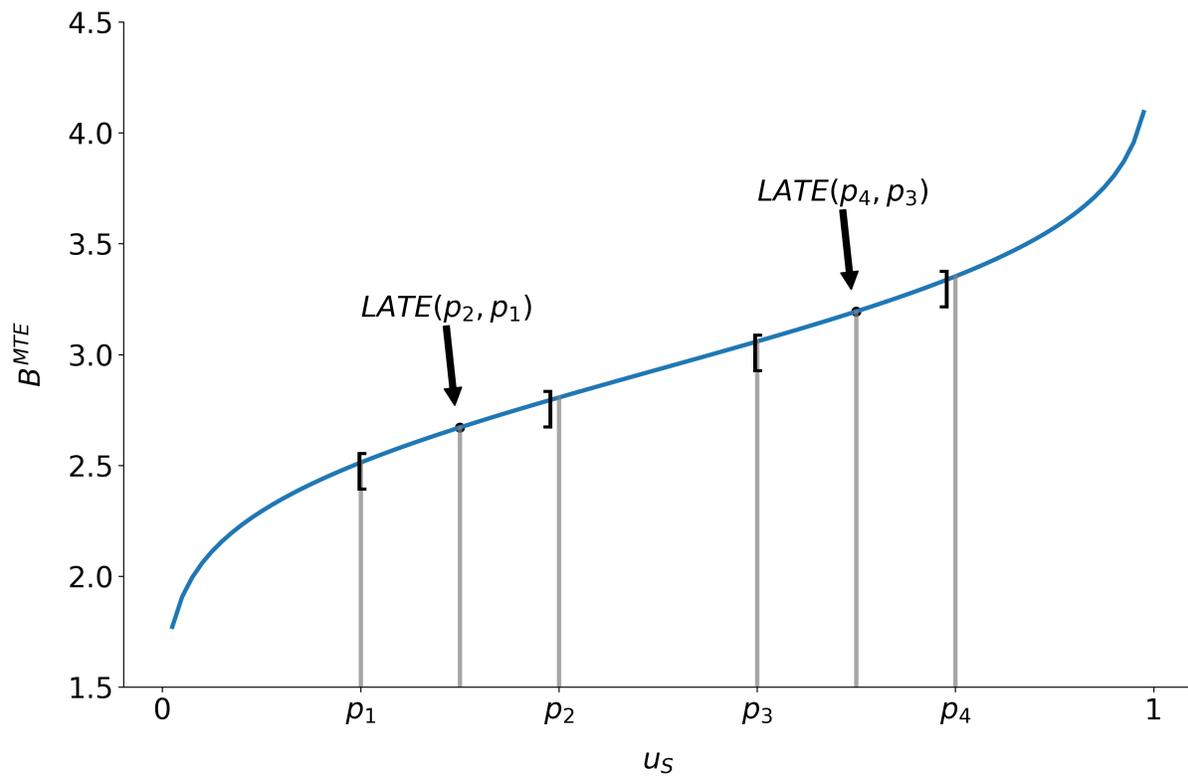


Fig. 2: **Fig. 2:** B^{LATE} at different values of u_S

The average effect of a policy and the average effect of a treatment are linked by the marginal treatment effect (B^{MTE}). The B^{MTE} was introduced into the literature by [4] and extended by [17], [18] and [19].

1.3.4 Marginal Treatment Effect

The B^{MTE} is the treatment effect parameter that conditions on the unobserved desire to select into treatment. Let V be the heterogeneity effect that impacts the propensity for treatment participation and let $U_S = F_V(V)$. Then, the B^{MTE} is defined as

$$B^{MTE}(u_S) = E[Y_1 - Y_0 | U_S = u_S].$$

The B^{MTE} is the average benefit for persons with observable characteristics $X = x$ and unobservables $U_S = u_S$. By construction, U_S denotes the different quantiles of V . So, when varying U_S but keeping X fixed, then the B^{MTE} shows how the average benefit varies along the distribution of V . For U_S evaluation points close to zero, the B^{MTE} is the average effect of treatment for individuals with a value of V that makes them most likely to participate. The opposite is true for high values of U_S . The B^{MTE} provides the underlying structure for all average effect parameters previously discussed. These can be derived as weighted averages of the B^{MTE} ([18]).

Parameter j , $\Delta j(x)$, can be written as

$$\Delta j = \int_0^1 B^{MTE}(u_S) \omega^j(u_S) du_S,$$

where the weights $\omega^j(u_S)$ are specific to parameter j , integrate to one, and can be constructed from data. For instance figure 3 shows weights for the B^{ATE} , B^{TT} and the B^{TUT} as well as the corresponding B^{MTE} . Contrary, figure 2 emphasizes that the concept of B^{LATE} is closely related to the idea of B^{MTE} . It illustrates that B^{LATE} evaluates B^{MTE} along a particular interval of the distribution of the unobservable Variable V . The specific range depends on the chosen instrument.

All parameters are identical only in the absence of essential heterogeneity. Then, the $B^{MTE}(x, u_S)$ is constant across the whole distribution of V as agents do not select their treatment status based on their unobservable benefits. This can be seen in figure 4 which illustrates B^{MTE} in the absence of essential heterogeneity, represented by the dotted orange line as well as an example for the B^{MTE} in the presence of essential heterogeneity portrayed by the blue graph.

So far, we have only discussed average effect parameters. However, these conceal possible treatment effect heterogeneity, which provides important information about a treatment. Hence, we now present their distributional counterparts ([1]).

1.4 Distribution of Potential Outcomes

Several interesting aspects of policies cannot be evaluated without knowing the joint distribution of potential outcomes ([2], [15]). The joint distribution of (Y_1, Y_0) allows to calculate the whole

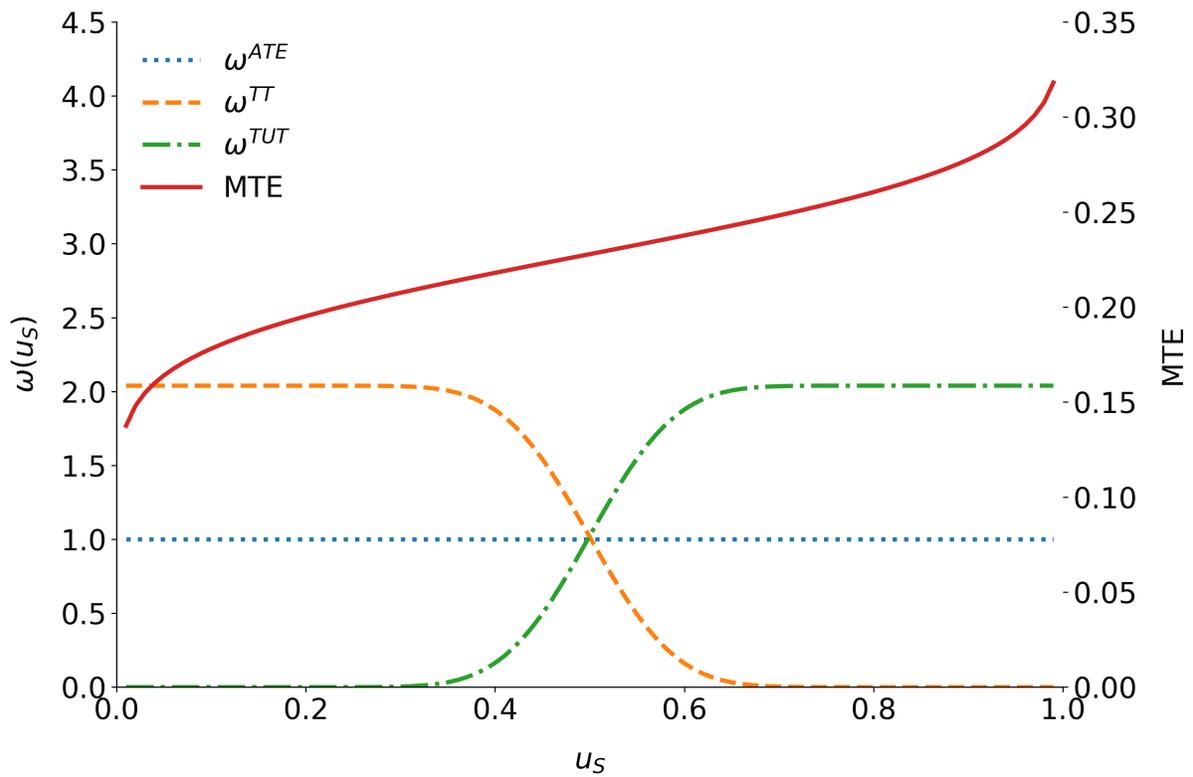


Fig. 3: **Fig. 3:** Weights for the marginal treatment effect for different parameters.

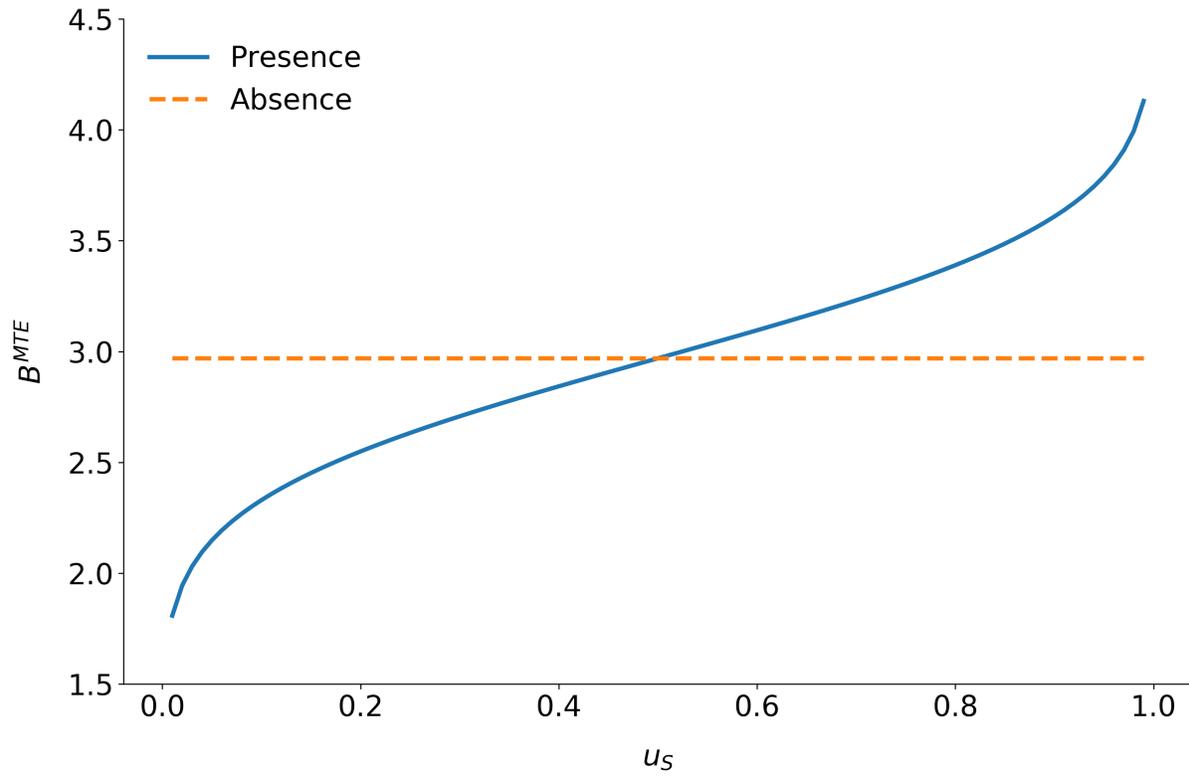


Fig. 4: **Fig 4:** B^{MTE} in the presence and absence of essential heterogeneity.

distribution of benefits. Based on it, the average treatment and policy effects can be constructed just as the median and all other quantiles. In addition, the portion of people that benefit from treatment can be calculated for the overall population $Pr(Y_1 - Y_0 > 0)$ or among any subgroup of particular interest to policy makers $Pr(Y_1 - Y_0 > 0|X)$. This is important as a treatment which is beneficial for agents on average can still be harmful for some. For a comprehensive overview on related work see [2] and the work they cite. The survey by [10] provides an overview about the alternative approaches to the construction of counterfactual observed outcome distributions. See [3], [29] and [30] for their studies of quantile treatment effects.

The zero of an average effect might be the result of part of the population having a positive effect, which is just offset by a negative effect on the rest of the population. This kind of treatment effect heterogeneity is informative as it provides the starting point for an adaptive research strategy that tries to understand the driving force behind these differences ([22], [23]).

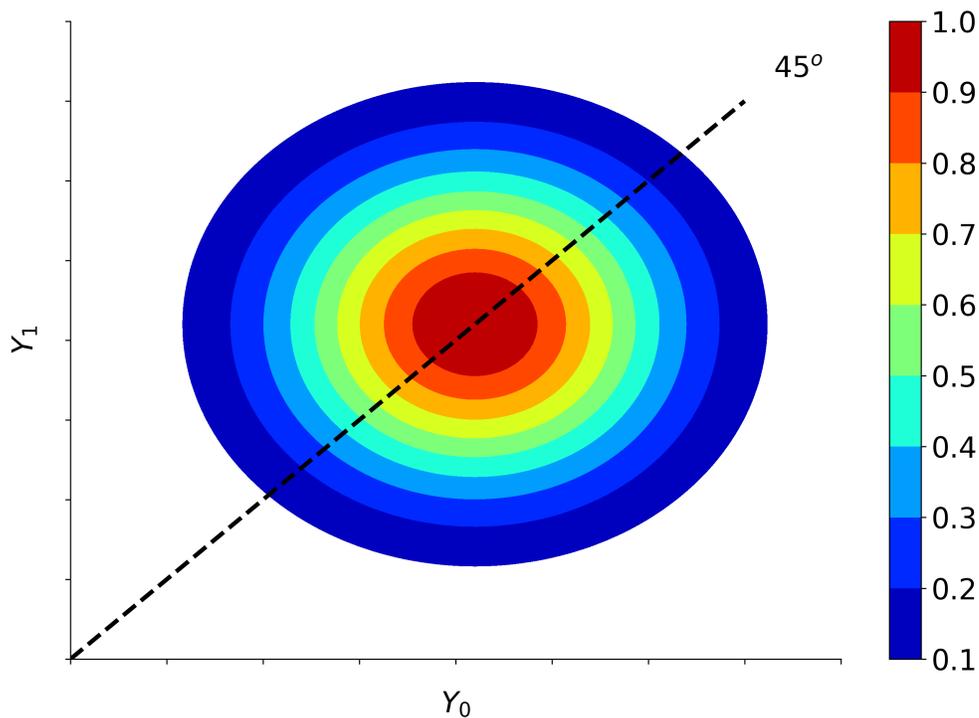


Fig. 5: **Fig 5:** Distribution of potential Outcomes

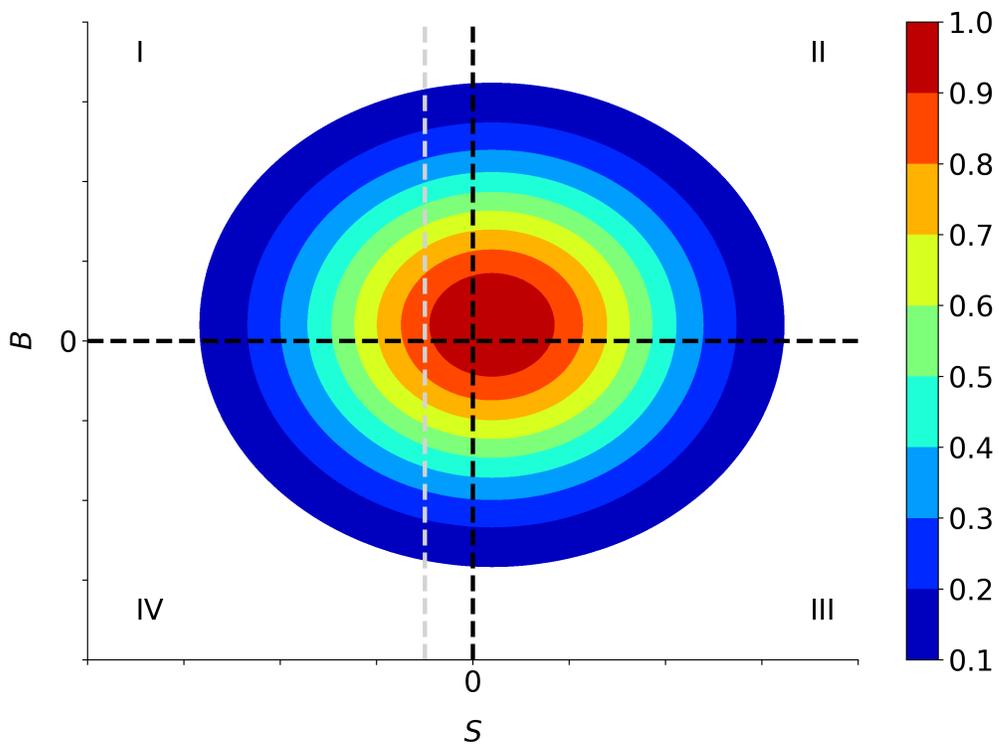


Fig. 6: **Fig. 6:** Distribution of benefits and surplus

The `grmpy` package can be conveniently installed from the [Python Package Index \(PyPI\)](#) or directly from its source files. We currently support Python 3.6+ on Linux systems.

2.1 Python Package Index

You can install the stable version of the package the usual way.

```
$ pip install grmpy
```

2.2 Source Files

You can download the sources directly from our [GitHub repository](#).

```
$ git clone https://github.com/OpenSourceEconomics/grmpy.git
```

Once you obtained a copy of the source files, installing the package in editable model is straightforward.

```
$ pip install -e .
```

2.3 Test Suite

Please make sure that the package is working properly by running our test suite using `pytest`.

```
$ python -c "import grmpy; grmpy.test()"
```

We now illustrate the basic capabilities of the `grmpy` package. We start with the assumptions about functional form and the distribution of unobservables and then turn to some simple use cases.

3.1 Assumptions

The `grmpy` package implements the normal linear-in-parameters version of the generalized Roy model. Both potential outcomes and the choice (Y_1, Y_0, D) are a linear function of the individual's observables (X, Z) and random components (U_1, U_0, V) .

$$\begin{aligned}Y_1 &= X\beta_1 + U_1 \\Y_0 &= X\beta_0 + U_0 \\D &= I[D^* > 0] \\D^* &= Z\gamma - V\end{aligned}$$

We collect all unobservables determining treatment choice in $V = U_C - (U_1 - U_0)$. The unobservables follow a normal distribution $(U_1, U_0, V) \sim \mathcal{N}(0, \Sigma)$ with mean zero and covariance matrix Σ . Individuals decide to select into latent indicator variable D^* is positive. Depending on their decision, we either observe Y_1 or Y_0 .

3.2 Model Specification

You can specify the details of the model in an initialization file ([example](#)). This file contains several blocks:

SIMULATION

The *SIMULATION* block contains some basic information about the simulation request.

| Key | Value | Interpretation |
|--------|-------|--|
| agents | int | number of individuals |
| seed | int | seed for the specific simulation |
| source | str | specified name for the simulation output files |

ESTIMATION

The *ESTIMATION* block determines the basic information for the estimation process.

| Key | Value | Interpretation |
|-------------|-------|---|
| agents | int | number of individuals (for the comparison file) |
| file | str | name of the estimation specific init file |
| optimizer | str | optimizer used for the estimation process |
| start | str | flag for the start values |
| maxiter | int | maximum numbers of iterations |
| dependent | str | indicates the dependent variable |
| indicator | str | label of the treatment indicator variable |
| output_file | str | name for the estimation output file |
| comparison | int | flag for enabling the comparison file creation |

TREATED

The *TREATED* block specifies the number and order of the covariates determining the potential outcome in the treated state and the values for the coefficients β_1 . Note that the length of the list which determines the paramters has to be equal to the number of variables that are included in the order list.

| Key | Container | Values | Interpretation |
|--------|-----------|--------|-----------------|
| params | list | float | Paramters |
| order | list | str | Variable labels |

UNTREATED

The *UNTREATED* block specifies the covariates that a the potential outcome in the untreated state and the values for the coefficients β_0 .

| Key | Container | Values | Interpretation |
|--------|-----------|--------|-----------------|
| params | list | float | Paramters |
| order | list | str | Variable labels |

CHOICE

The *CHOICE* block specifies the number and order of the covariates determining the selection process and the values for the coefficients γ .

| Key | Container | Values | Interpretation |
|--------|-----------|--------|-----------------|
| params | list | float | Parameters |
| order | list | str | Variable labels |

DIST

The *DIST* block specifies the distribution of the unobservables.

| Key | Container | Values | Interpretation |
|--------|-----------|--------|---|
| params | list | float | Upper triangular of the covariance matrix |

VARTYPES

The *VARTYPES* section enables users to specify optional characteristics to specific variables in their simulated data. Currently there is only the option to determine binary variables. For this purpose the user have to specify a key which reflects the corresponding variable label and assign a list to this label which contains the type (*binary*) as a string as well as a float (<0.9) that determines the probability for which the variable is one.

| Key | Container | Values | Interpretation |
|-----------------------|-----------|------------------|---|
| <i>Variable label</i> | list | string and float | Type of variable + additional information |

SCIPY-BFGS

The *SCIPY-BFGS* block contains the specifications for the *BFGS* minimization algorithm. For more information see: [SciPy documentation](#).

| Key | Value | Interpretation |
|------|-------|--|
| gtol | float | the value that has to be larger as the gradient norm before successful termination |
| eps | float | value of step size (if <i>jac</i> is approximated) |

SCIPY-POWELL

The *SCIPY-POWELL* block contains the specifications for the *POWELL* minimization algorithm. For more information see: [SciPy documentation](#).

| Key | Value | Interpretation |
|------|-------|--|
| xtol | float | relative error in solution values x_{opt} that is acceptable for convergence |
| ftol | float | relative error in $\text{fun}(x_{opt})$ that is acceptable for convergence |

3.3 Examples

In the following chapter we explore the basic features of the `grmpy` package. The resources for the tutorial are also available [online](#). So far the package provides the features to simulate a sample from the generalized Roy model and to estimate some parameters of interest for a provided sample as specified in your initialization file.

Simulation

First we will take a look on the simulation feature. For simulating a sample from the generalized Roy model you use the `simulate()` function provided by the package. For simulating a sample of your choice you have to provide the path of your initialization file as an input to the function.

```
import grmpy

grmpy.simulate('tutorial.grmpy.yml')
```

This creates a number of output files that contain information about the resulting simulated sample.

- **data.grmpy.info**, basic information about the simulated sample
- **data.grmpy.txt**, simulated sample in a simple text file
- **data.grmpy.pkl**, simulated sample as a pandas data frame

Estimation

The other feature of the package is the estimation of the parameters of interest. The specification regarding start values and the optimizer options are determined in the *ESTIMATION* section of the initialization file.

```
grmpy.fit('tutorial.grmpy.yml')
```

As in the simulation process this creates a number of output file that contains information about the estimation results.

- **est.grmpy.info**, basic information of the estimation process
- **comparison.grmpy.txt**, distributional characteristics of the input sample and the samples simulated from the start and result values of the estimation process

The following section illustrates the reliability of the estimation strategy behind the `grmpy` package when facing agent heterogeneity and shows also that the corresponding results withstand a critical examination. The checks in both subsections are based on a mock `data set` respectively the `estimation results` from

Carneiro, Pedro, James J. Heckman, and Edward J. Vytlačil. `Estimating Marginal Returns to Education`. *American Economic Review*, 101 (6):2754-81, 2011.

We conduct two different test setups. Firstly we show that `grmpy` is able to provide better results than simple estimation approaches in the presence of essential heterogeneity. For that purpose we rely on a monte carlo simulation setup which enables us to compare the results obtained by the `grmpy` estimation process with such of a standard Ordinary Least Squares (OLS) approach. Secondly we show that `grmpy` is capable of replicating the B^{MTE} results by [6] for the parametric version of the Roy model.

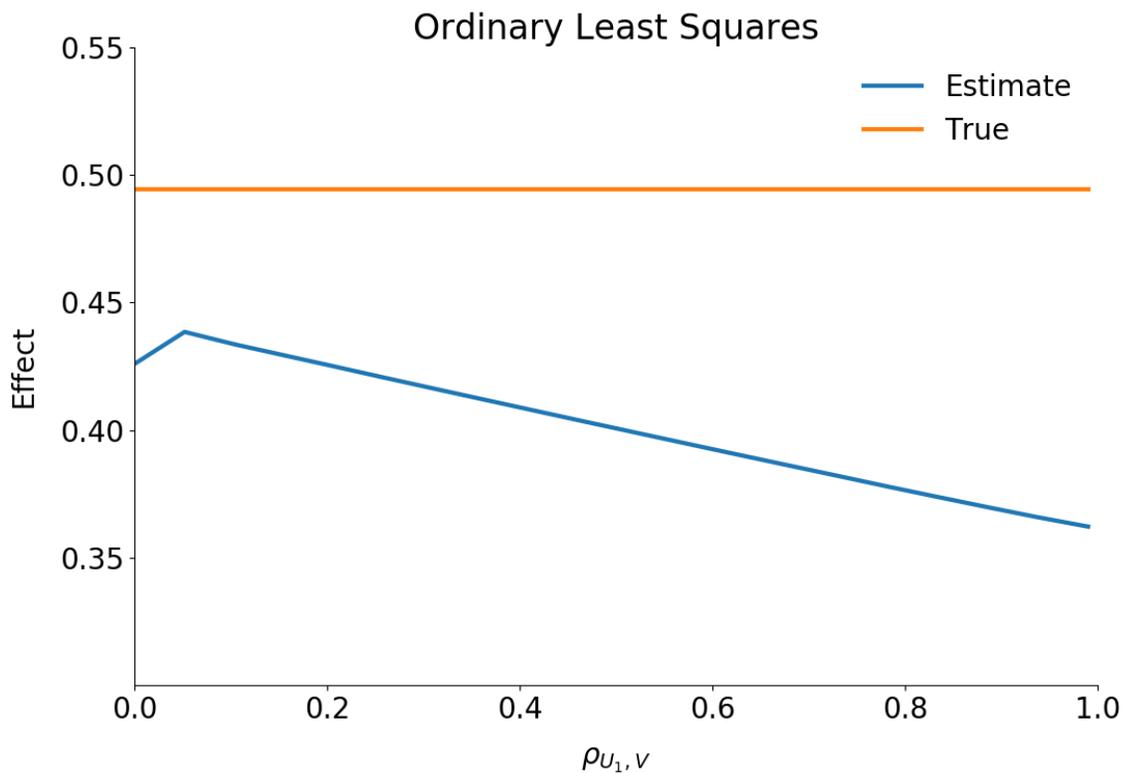
4.1 Reliability of Estimation Results

The estimation results and data from [6] build the basis of the reliability test setup. The data is extended by combining them with simulated unobservables that follow a distribution that is pre-specified in the following `initialization file`. In the next step the potential outcomes and the choice of each individual are calculated by using the estimation results.

This process is iterated a certain amount of times. During each iteration the rate of correlation between the simulated unobservables increases. Translated in the Roy model framework this is

equivalent to an increase in the correlation between the unobservable variable U_1 and V , the unobservable that indicates the preference for selecting into treatment. Additionally the specifications of the distributional characteristics are designed so that the expected value of each unobservable is equal to zero. This ensures that the true B^{ATE} is fixed to a value close to 0.5 independent of the correlation structure.

For illustrating the reliability we estimate B^{ATE} during each step with two different methods. The first estimation uses a simple OLS approach.

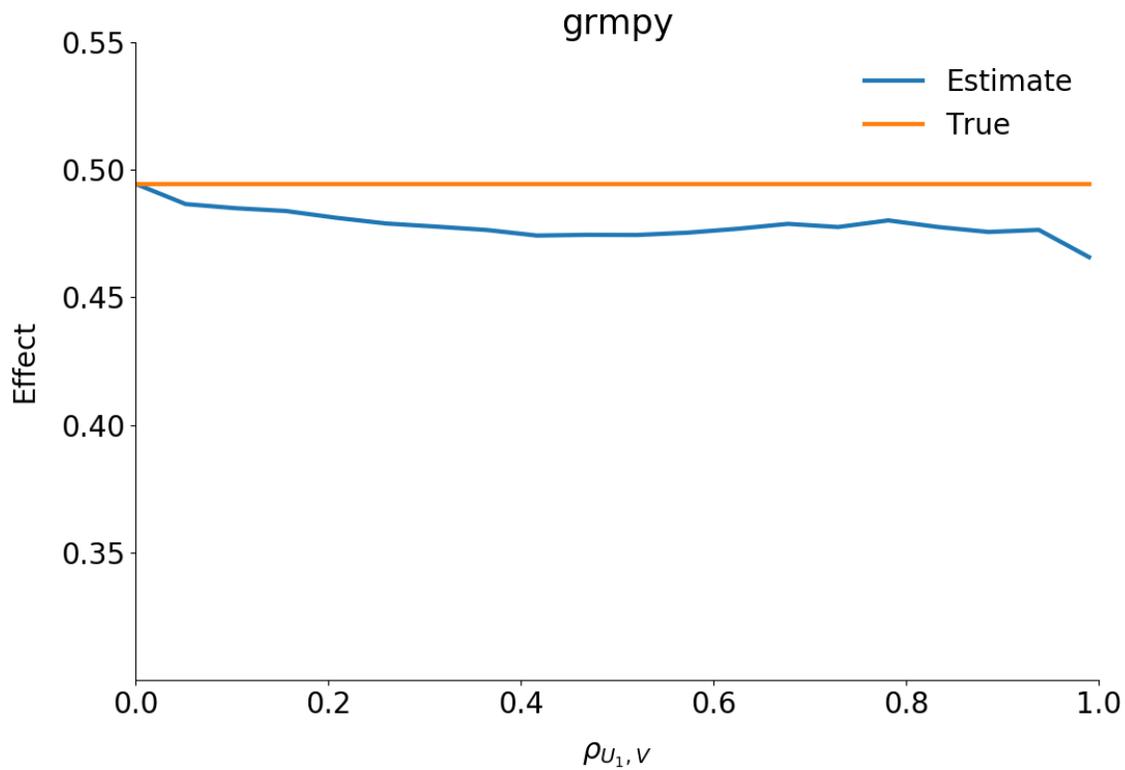


As can be seen from the figure, the OLS estimator underestimates the effect significantly. The stronger the correlation between the unobservable variables the more or less stronger the downwards bias.

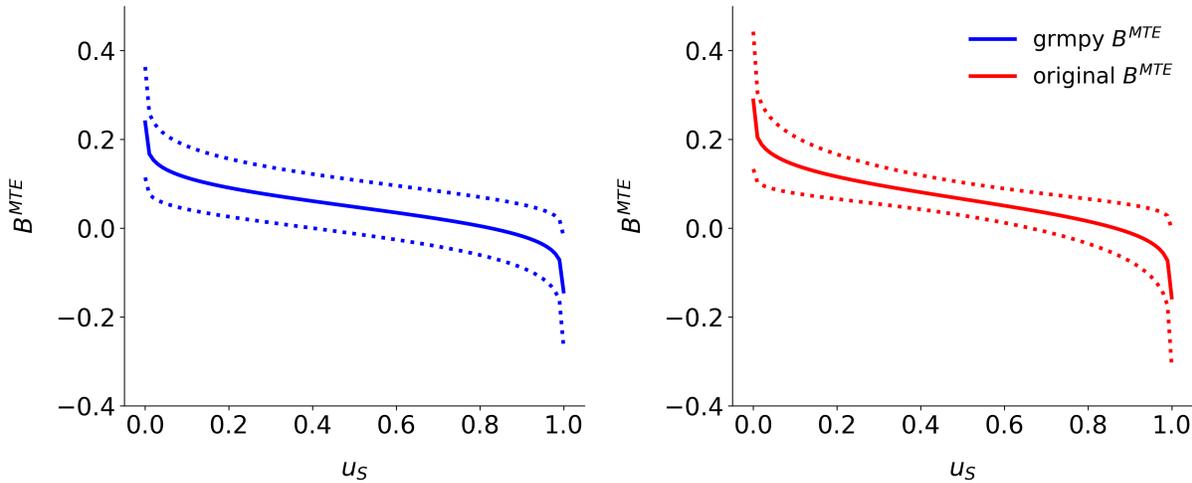
The second figure shows the estimated B^{ATE} from the `grmpy` estimation process. Conversely to the OLS results the estimate of the average effect is close to the true value even if the unobservables are almost perfectly correlated.

4.2 Replication

The second check of reliability compares the results of our estimation process with already existing results from the literature. For this purpose we replicate the results for the marginal treatment effect from Carneiro 2011 ([6]). Additionally we provide a [jupyter notebook](#) that runs an estimation



based on an [initialization file](#) for easy reconstruction of our test setup. The init file corresponds to the specifications of the authors. As shown in the figure below the results are really close to the original results. The deviation seems to be negligible because of the usage of a mock dataset.



We now briefly discuss our software engineering practices that help us to ensure the transparency, reliability, scalability, and extensibility of the `grmpy` package. Please visit us at the [Software Engineering for Economists Initiative](#) for an accessible introduction on how to integrate these practices in your own research.

5.1 Test Battery

We use `pytest` as our test runner. We broadly group our tests in three categories:

- **property-based testing**

We create random model parameterizations and estimation requests and test for a valid return of the program.

- **reliability testing**

We conduct numerous Monte Carlo exercises to ensure that we can recover the true underlying parameterization with an estimation. Also by varying the tuning parameters of the estimation (e.g. random draws for integration) and the optimizers, we learn about their effect on estimation performance.

- **regression testing**

We provide a regression test. For this purpose we generated random model parameterizations, simulated the corresponding outputs, summed them up and saved

both, the parameters and the sums in a json file. The json file is part of the package. Through this the provided test is able to draw parameterizations randomly from the json file. In the next step the test simulates the output variables and compares the sum of the simulated output with the associated json file information. This ensures that the package works accurate even after an update to a new version.

5.2 Documentation

The documentation is created using [Sphinx](#) and hosted on [Read the Docs](#).

5.3 Code Review

We use several automatic code review tools to help us improve the readability and maintainability of our code base. For example, we work with [Codacy](#). However, we also conduct regular peer code-reviews using [Reviewable](#).

5.4 Continuous Integration Workflow

We set up a continuous integration workflow around our [GitHub Organization](#). We use the continuous integration services provided by [Travis CI](#). `tox` ensures that the package installs correctly with different Python versions.

Great, you are interested in contributing to the package.

To get acquainted with the code base, you can check out our [issue tracker](#) for some immediate and clearly defined tasks. For more involved contributions, please see our roadmap below. All submissions are required to follow this project-agnostic [contribution guide](#)

6.1 Roadmap

We aim for improvements to the `grmpy` package in four domains: Objects of Interest, Estimation Methods, and Numerical Methods.

6.1.1 Objects of Interest

- adding marginal surplus and marginal cost parameters as presented by [\[9\]](#)

6.1.2 Estimation Methods

- implement polynomial and local-instrumental variable estimation as outlined by [\[16\]](#)
- implementing capability to control for unobservables by adding a factor structure assumption as in [\[8\]](#)

6.1.3 Program Structure

- refactoring code to incorporate elements of object-oriented programming

6.1.4 Numerical Methods

- exploring alternative optimization algorithms to address large estimation tasks

CHAPTER 7

Contact and Credits

If you have any questions or comments, please do not hesitate to [contact us](#) directly.

7.1 Development Lead

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7.3 Acknowledgments

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7.3.1 Suggested Citation

We appreciate citations for `grmpy` because it helps us find out how people have been using the package and it motivates further work. Please use our Digital Object Identifier (DOI) and see [here](#) for further citation styles.

CHAPTER 8

Changes

This is a record of all past `grmpy` releases and what went into them in reverse chronological order. We follow [semantic versioning](#) and all releases are available on [PyPI](#).

8.1 1.0.0 - 2018-XX-XX

This is the initial release of the `grmpy` package.

CHAPTER 9

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